The Crystal Structure of Di(Histidino)Zinc Pentahydrate

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The crystal structure of di(histidino)zinc pentahydrate, $Zn(C_6H_8N_3O_2)_2.5H_2O$, has been determined by Fourier analysis and least-squares refinement using three-dimensional intensity data from $CuK\alpha$ radiation. The crystals are monoclinic, with space group C2/c, and cell dimensions

$$a = 16.41, b = 14.755, c = 10.99 \text{ Å}, \beta = 129.6^{\circ}.$$

The primary co-ordination around the zine atoms, which lie on two-fold axes, is a distorted tetrahedron, consisting of an amino nitrogen and an imidazole nitrogen (at 2.05 and 2.00 Å) from each of the two histidine groups. One oxygen atom from each histidine group is also very weakly associated (at 2.91 Å). The molecules of di(histidino)zinc and the water molecules take part in an elaborate system of hydrogen bonds holding the structure together.

Some evidence (Tanford & Epstein, 1954) suggested that in the association of zinc with insulin, histidine residues are involved; thus a knowledge of the structure of di(histidino)zinc seemed relevant to the studies of crystalline zinc insulin which are in progress in this laboratory. This, and a general interest in the coordination chemistry of both zinc and histidine

$$\underset{\mathrm{HN}}{\overset{\mathrm{NH}_{2}}{\longrightarrow}} -\mathrm{CH}_{2} -\mathrm{CH} \overset{\mathrm{NH}_{2}}{\overset{\mathrm{COOH}}{\longleftarrow}}$$

led us to undertake the structure determination. Some recent evidence (Marcker, 1960), however, suggests that it is not histidine, but the *N*-terminal phenylalanine of insulin which is co-ordinated to zinc.

The crystals whose structure determination we shall describe were prepared from DL-histidine and have the composition $Zn(C_6H_8N_3O_2)_2.5$ H₂O. Kretsinger, Cotton & Bryan (1963) have studied crystals of $Zn(C_6H_8N_3O_2)_2.2$ H₂O prepared from L-histidine, and this structure determination is described in the following paper.

Crystal data

Crystals were obtained by slowly cooling an aqueous solution of zinc sulphate and DL-histidine (Weitzel *et al.*, 1957). Oscillation and Weissenberg photographs were taken with Cu $K\alpha$ radiation. For determination of the cell dimensions an oscillation camera with the film mounted according to Straumanis's method, and the extrapolation procedure described by Henry, Lipson & Wooster (1960), were used. The crystals are monoclinic, elongated along *c*.

$$a = 16.41 \pm 0.015, \ b = 14.755 \pm 0.015, c = 10.99 \pm 0.015 \text{ Å}; \ \beta = 129.6 \pm 0.15^{\circ}.$$

From systematic absences the space group is C2/c

or Cc; a statistical test (Wilson, 1949) on the hk0intensity data indicated the centrosymmetric group C2/c, and throughout the subsequent structure determination this appeared to be satisfactory. The density, measured by flotation, is 1.504 g.cm⁻³, so there are four molecules per unit cell (the calculated density is 1.502 g.cm⁻³).

Structure determination

Multiple-film Wiessenberg photographs were taken of the layers h0l to h8l and hk0 to hk4, the intensities measured visually, and Lp corrections applied. Fivesixths of the reflections in the higher layers were measured as 'extended spots' and one-sixth as 'contracted spots'. Those reflections which could be measured in both extended and contracted forms on any one film were used to select an empirical spot-shape correction. The required correction, δ , as a fraction of the measured intensity is, to a good approximation. $(I_{\text{cont}}-I_{\text{ext}})/2I_{\text{mean}}$. In any layer it should be largest at $\xi \sim 0$ and decrease to zero at the edge of the film, *i.e.* at $\theta = 90^{\circ}$ (θ is the Bragg angle, and ξ and ζ are reciprocal lattice co-ordinates). Various plots were made to find a linear relation between δ in any one layer, and some function of θ or ξ ; three examples are given in Fig. 1. $V(\sin \theta')$ was chosen (where $\sin \theta' = \xi/2$, but $\sin \theta'$, $\sin \theta$, $\sqrt{(\sin \theta)}$ are not significantly less satisfactory since the errors in measurement of δ are considerable; $\cos \theta$, however, does seem to be much less satisfactory. Further, the slope of δ with respect to the chosen function of θ , should change smoothly with ζ , the layer height; here the slopes in all layers could be adequately represented by ζ multiplied by a single constant k. Thus the intensities were corrected in the following way:

$$I_{\text{ext}} \times (1 + k\zeta \sqrt{(\sin \theta')} + K)$$
$$I_{\text{cont}} \times (1 - k\zeta \sqrt{(\sin \theta')} + K)$$

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Fig. 1. Examples of plots, for the layer hk3, of $(I_{\text{cont}}-I_{\text{ext}})/I_{\text{mean}}$ which is equivalent to twice the required spot-shape correction (expressed as a fraction of I). The larger circles represent $\theta = 90^{\circ}$ where the spot-shape correction should be zero.

k is one constant for all the data (=0.67 here),

K are normalising constants in each layer, to make the correction zero at $\theta = 90^{\circ}$.

After this spot-shape correction, all the data were correlated and assembled. The intensities of 1370 reflections were measured, those of 557 were too small for observation, and about 300 were not recorded on any film, although they are within the Cu $K\alpha$ limit. An approximate scale and temperature factor were determined from a 'Wilson plot'.

Sharpened Patterson projections along the b and caxes gave tentative positions for the zinc atoms, which were confirmed by the three-dimensional Patterson synthesis, sharpened 'to point atoms at rest'. The zinc atoms are on two-fold axes at $0, y, \frac{1}{4}$, 0, -y, $\frac{3}{4}$, etc., with y=0.037. By superposition of the Patterson sections from these two positions as origins, the positions of all atoms of the histidine residue (except hydrogen) were found (Fig. 2). From the smaller peaks three reasonable water-molecule oxygen positions were found, one being on a two-fold axis. The only other features in the superposition map were diffraction peaks around the zinc atom, and one small peak too near to other atomic positions to be a water molecule. Structure factors were calculated and gave $R = \Sigma ||F_0| - |F_c||/\Sigma |F_o| = 21\%$, for all observed re-



Fig. 2. Superposition of the sharpened three-dimensional Patterson series from the zinc atom at 0, 0.037, 0.25, as origin (full lines) and from the zinc atom at 0, -0.037, 0.75, as origin (dotted lines). The section at x=13/60 is shown; the crosses mark the positions of C_3 , N_3 , and C_6' which all lie in or near this section.

flections. Comparison of the positions with the coordinates subsequently found after refinement showed that C₂, which is nearly in the glide plane, had been misplaced by 0.15 Å; no other atom was more than 0.1 Å from its correct position, and the average displacement was 0.05 Å.

Refinement

Two $(F_o - F_c)$ series were calculated and appropriate changes made to the co-ordinates, scale, and temperature factors. R fell to 18%. The hydrogen atoms of the histidine group (at the expected positions) were included in the next and subsequent structure-factor calculations, and the co-ordinates and individual isotropic temperature factors of zinc, carbon, nitrogen, and oxygen atoms were refined by least squares. At the end of this refinement R was 12.7%.

To confirm the hydrogen positions already used, and to find others, another $(F_o - F_c)$ series was calculated in which no hydrogen contributions were included in F_c . Positive regions of electron density appeared in most places where hydrogen atoms of the histidine group were expected. For many of the hydrogen atoms of water molecules there are two alternative sites; such 'half' hydrogens were much less easy to find. It was evident that the largest features in the difference series were not due to hydrogen atoms but to anisotropic vibrations of the other atoms.

Three cycles of anisotropic least-squares refinement were then carried out, bringing R to 10.5% (for observed reflections only), and the co-ordinate shifts

Table 1(a). Positional and thermal parameters, determined by anisotropic least-squares refinement

The numbering of the atoms can be seen in Figs. 3 and 6

The temperature factor of an atom is

exn	$-(h_{\rm r})$	$h^{2} + l$	$b_{aa}k^2 +$	$b_{aa}l^2$	$+b_{\alpha}$	kl +	bark	l+	b	hk)
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			-						
	x	y	z	b_{11}	b_{22}	b_{33}	b_{23}	b_{31}	b_{12}
Zn	0	0.03718	0.2500	0.00288	0.00208	0.00925	0	0.00598	0
C.	0.1733	0.0767	0.6328	0.00476	0.00220	0.01056	0.00155	0.01099	-0.00117
Č.	0.1908	-0.0097	0.5775	0.00442	0.00217	0.00826	-0.00236	0.00873	0.00001
\tilde{C}_{-}^{2}	0.2626	0.0094	0.5354	0.00313	0.00373	0.00895	-0.00171	0.00751	-0.00053
C.	0.2286	0.0891	0.4302	0.00376	0.00318	0.00854	-0.00263	0.00932	-0.00092
C_{-}^{4}	0.1217	0.1842	0.2346	0.00634	0.00250	0.01074	-0.00096	0.01360	-0.00089
\tilde{C}_6^5	0.2887	0.1553	0.4341	0.00505	0.00411	0.01133	-0.00446	0.01137	-0.00329
N.	0.0894	-0.0481	0.4403	0.00364	0.00243	0.01019	0.00213	0.00855	-0.00159
N.	0.1217	0.1079	0.2989	0.00369	0.00259	0.00761	-0.00089	0.00837	-0.00010
N ₃	0.2197	0.2135	0.3116	0.00871	0.00336	0.01559	-0.00332	0.01869	-0.00368
0.	0.0821	0.1071	0.5572	0.00504	0.00299	0.01765	-0.00716	0.01252	-0.00156
$\tilde{0}$	0.2534	0.1141	0.7554	0.00713	0.00289	0.00913	-0.00403	0.01011	-0.00205
$\tilde{0}$	0.1557	0.2152	0.8665	0.01227	0.00465	0.02847	0.00134	0.02996	0.00166
0 <u>3</u>	0.0344	0.4097	0.0148	0.00597	0.01076	0.02138	-0.00685	0.00837	0.00491
Ŭ₌	0	0.3424	0.7500	0.00958	0.00519	0.01546	0	0.01513	0

Table 1(b). Coordinates and temperature factors of hydrogen atoms used in structure factor calculations

	x	\boldsymbol{y}	z	B	On atom
н.	0.234	-0.052	0.680	3.5 Å^{-2}	C,
H.	0.120	-0.108	0.425	3.5	N,
\mathbf{H}_{n}^{2}	0.028	-0.072	0.433	3.5	N ₁
нÅ	0.338	0.000	0.579	3.5	C_3
H.	0.212	-0.042	0.400*	3.5	$\tilde{C_3}$
H,	0.052	0.217	0.132	3.5	C_5
н°	0.230	0.273	0.295	3.5	N_3
н,	0.374	0.161	0.518	3.5	C_6
н°	0.192	0.500	0.825	6.0	O_3
H	0.108	0.400	0.088	6.0	O_4
μH.,	0.220	0.247	0.962	6.0	O ₃
åH,	0.100	0.267	0.825	6.0	O_3
λ ¹	0.050	0.300	0.762	6.0	O_5
ÅH.	0.008	0.465	0.005	$6 \cdot 0$	O_4
ĨН.	0.025	0.384	-0.080	6.0	O_4
iH.	0.020	0.380	0.839	6.0	O_5

* This coordinate was actually used in structure factor calculation, but should have been 0.4300.

indicated by a fourth cycle were all less than 0.0015 Å. These parameters are given in Table 1, and the observed and calculated structure factors in Table 2(a). When non-observed reflections are included R is 13.7% (Table 2(b)).

The atomic scattering factors used for carbon, nitrogen, and oxygen were those of Berghuis *et al.* (1955); O₁ and O₂, the carboxyl oxygen atoms were treated as $O^{\frac{1}{2}-}$. For hydrogen, McWeeny's (1951) scattering factor was used, and for zinc that of Thomas & Umeda (1957) with a correction for anomalous dispersion (Dauben & Templeton, 1955).

J. S. Rollett's 'Structure Factor and Least Squares' refinement program was used; reflections were given weights $|F_o|/960$ when $|F_o| < 960$ (on the same scale as in Table 2), and $960/|F_o|$ otherwise. This and all the other calculations were done on the Ferranti 'Mercury' Computer at Oxford.

Standard deviations, calculated according to Ahmed and Cruickshank's formula (1953) (with Darlow's (1960) correction), are given in Table 3(a). In Table 3(b) the bond distances obtained at the end of the isotropic refinement are given for comparison with those obtained after the anisotropic refinement. There are small differences, but the largest (C_2-C_3) is 0.015 Å, and is smaller than the standard deviation of either. The same is true of bond angles. Thus three cycles of anisotropic least-squares refinement achieved an improvement in R, but no significant change in interatomic distances or angles, and only slightly smaller standard deviations in these distances and angles.

Description and discussion of the structure

The configuration of the molecule, and bond lengths and angles are shown in Fig. 3. The angles around the zinc atom are given in Table 4; bond lengths are also given in Table 3(b).

The primary co-ordination group around the zinc atom is a distorted tetrahedron, consisting of an amino nitrogen and an imidazole nitrogen from each of two Table 2(a). Observed and calculated structure factors

The columns represent h, $50F_o$, $50F_c$. The lines preceded by an asterisk give the indices l and k for the group of reflections immediately below

• 5 7		- 15 -947	-890	-2	580	6 13	-13 707	747	-16 -374	-305	o -395	-404	• 11 7	
1 -120	9 - 988	- 17 -424	-282	-4	12 90	13 17	-15 777	698	• 9 3		-3 -383	-234	-7 030	717
3 - 104	7 ~ 999	- 19 - 268	- 2 15	-6	329	503	-17 693	030	-3 -1030	- 10 37	-4 -438	-529	-9 017 4	431
7 -40	5 -406	• 6 4		-8	~335	-450	-19 840	1015	-7 -400	-275	~10 -915	-912	-13 876	200
-1 -135	9 -1344	2 -1045	- 1033	- 10	1796	1935			-9 -390	- 30 1	-13 -1105	-1063	470	434
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-5 -156	5 -1578	-3 - 16 34	- 14 39	- 14	645	552	2 290	34 1	-13 -951	-959	- 18 - 593	-596	-6 310	357
-7 -190	9 - 1947	-4 -347	-345	- 18	529	453	4 383	351	- 19 -409	-450	• 10 3		-8 410	432
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2 - 103	6 - 1075	-1 544	672	-7	1435	1491	-16 573	487	-18 -341	-#33	-17 -341	-247	-14 031	930
4 -84	1 -94 I	-5 -1158	-919	-9	2 15 3	1951	~18 654	574	-20 -329	-431	-19 -544	-588	-10 004	400
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-10 -11	- 177	• 6 8		-9	13 18	11 95	- 16 358	327	-1 -559	-626	-13 329	4 5 I	• 13 5	
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$\begin{array}{c} 3 & -43 \\ 5 & -67 \\ 9 & -19 \\ -1 & -338 \\ -3 & -161 \\ -5 & -100 \\ -7 & -81 \end{array}$	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	-3 1068 -6 8 10 -8 555 -14 696 -16 316 * 7 1 3 390 -1 643	1005 846 522 738 196 193 6 18	- 15 - 17 • 7 - 4 - 6 - 8	350 843 410 8 1190 541 1317 639 2311	7 11 338 1169 620 1199 644 2389	-30 8 5 1 590 -7 8 10 -9 1074 -11 -430 -13 767 -15 34 1 - 8 6	70 3 698 94 t -5 27 7 33 3 2 3	$\begin{array}{c} -7 & -673 \\ -9 & -693 \\ -11 & 569 \\ -15 & -1355 \\ -15 & -953 \\ -17 & -813 \\ 9 & 8 \\ 0 & -456 \end{array}$	-584 -744 237 -977 -861 -712	-17 447 • 11 3 -4 261 -6 544 -14 563 -15 443 • 11 3 -3 238 -5 510	4 37 35 3 6 4 3 6 7 9 5 4 6 1 4 9 5 3 7	$\begin{array}{cccc} -9 & 36 \\ -17 & 4 \\ 10 & 5 \\ -16 & 238 \\ -16 & 238 \\ -16 & -245 \\ -15 & -345 \\ -13 & 1 \\ -13 & -337 \end{array}$	137 549 350 - 154 - 151
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$	$\begin{array}{rrrr} 9 & -1335 \\ 4 & -500 \\ 0 & -723 \\ 0 & -338 \\ 6 & -3469 \\ 7 & -1874 \\ 8 & -1144 \\ 0 & -1034 \\ 5 & -1611 \\ 3 & -3170 \end{array}$	$\begin{array}{cccc} -3 & 1068 \\ -6 & 810 \\ -8 & 555 \\ -14 & 696 \\ -16 & 316 \\ +7 & 1 \\ 3 & 290 \\ -1 & 643 \\ -9 & 363 \\ -11 & 590 \end{array}$	1005 846 521 738 196 193 618 299 635	- 13 - 17 - 17 - 17 - 17 - 17 - 7 - 2 - 4 - 6 - 78 - 10 - 12	350 843 410 8 1190 541 1317 639 2311 456 1238	7 11 3 38 1 169 6 20 1 199 6 44 3 389 4 79 1 246	-300 $300-300$ 8 $5-7$ $810-9$ $1074-11$ $-430-13$ $767-15$ $341-8$ 63 $438-6$ -559	70 3 698 94 t -527 7 33 32 3 567 -6 17	$\begin{array}{c} 3 & -673 \\ -9 & -693 \\ -11 & 569 \\ -13 & -135 \\ -17 & -813 \\ -17 & -813 \\ 0 & -456 \\ -2 & -385 \\ -4 & -569 \end{array}$	-584 -744 237 -977 -861 -723 -656 -474 -451	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	4 37 353 643 679 546 149 537 378 660	$\begin{array}{c} -9 & 36 \\ -17 & 410 \\ \bullet & 13 & 6 \\ -16 & 328 \\ \bullet & 13 & 8 \\ \bullet & 15 & -345 \\ \bullet & 13 & 1 \\ -13 & -337 \\ \bullet & 13 & 3 \\ -13 & -368 \end{array}$	137 549 350 - 24 - 15 1 - 264
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Fig. 3. Bond lengths and angles in one molecule of di(histidino)zinc, viewed along the two-fold axis. The bond angles around the zinc atom are given in Table 4.

histidine groups. But there is also one oxygen atom from each histidine group 2.91 Å from the zinc atom, which suggests a weak association. The two histidine groups are related by a two-fold axis through the zinc atom; thus the crystal contains molecules of di(D-histidino)zinc and of di(L-histidino)zinc related to each other by centres of symmetry.

With oxygen- or nitrogen-containing ligands zinc is frequently found in regular, or nearly regular, octahedral co-ordination, for example in zinc oxinate (Merritt, Cady & Mundy, 1954). But the co-ordination group found here in di(histidino)zinc closely resembles that in zinc salicylate dihydrate (Klug, Alexander & Sumner, 1958), where the zinc atom has four near neighbours (oxygen atoms at 2.03 and 2.06 Å) and two more oxygen atoms are further away (at 2.52 Å).

The arrangement of each histidine group with respect to the zinc atom is very nearly the same in these molecules as it is in the molecules described by Kretsinger, Cotton & Bryan (KC&B); the arrangement of four nitrogen atoms around zinc is also similar in the



Fig. 4. c-axis projection of one molecule of di(L-histidino)zinc. This projection is perpendicular to the two-fold axis through zinc and is to be compared with Fig. 4 of Kretsinger, Cotton & Bryan.

Table 2(b). Structure factors for non-observed reflections are given in the same form as in Table 2(a) except that F_{o} is replaced by the square root of half the minimum observable intensity multiplied by the appropriate L_{p} factor

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Table 3(a). Standard Deviations

	Anisotropic refinement	Isotropic refinement
Bonds between zinc and nitrogen or oxygen Bonds between carbon	0·012 Å	0·014 Å
nitrogen and oxygen Bond angles	0·020 Å 1·3°	0·023 Å 1·5°

two molecules, but the relation of one histidine group to the other is not. This can be seen by comparing Fig. 4 here with Fig. 4 in their paper. The KC&B molecule can be obtained (approximately) by rotating one histidine group in our molecule through 180° so that N_1 and N_2 replace each other.

The conformation of the histidine group can be compared with that in histidine hydrochloride (Donohue, Lavine & Rollett, 1956). The chief difference results from a rotation around the bond C₃-C₄, of the imidazole ring relative to the rest of the molecule

Table 3(b). Bond distances within the di(histidino)zinc molecule

-13 -63 61 -256

	Anisotropic	Isotropic
	refinement	refinement
Zn-N,	$2 \cdot 000$ Å	1·994 Å
Zn-N	2.049	2.046
Zn-O	2.912	2.900
C101	1.243	1.241
$C_1 - O_9$	1.260	1.263
$C_1 - C_2$	1.519	1.518
$C_{2}-N_{1}$	1.473	1.474
$C_2 - C_3$	1.539	1.554
$C_3 - C_4$	1.486	1.495
$C_4 - N_2$	1.417	1.412
$C_4 - C_6$	1.369	1.361
$N_2 - C_5$	1.329	1.337
$C_5 - N_3$	1.324	1.313
$C_6 - N_3$	1.374	1.375

(Fig. 5). This rotation allows both N_1 and N_2 to be co-ordinated to the zinc atom.

C3 and the atoms of the imidazole ring are coplanar within the limits of accuracy of the structure





Fig. 5. Projection along the bond C_3-C_4 of the histidine group in histidine hydrochloride (full lines) and in di(histidino)zinc (dotted lines). Double lines represent the plane of the imidazole ring.

determination; the largest calculated displacement from the mean plane is 0.013 Å. This plane is

$$9.700x - 8.023y - 9.186z + 2.442 = 0$$
.

The zinc atom, however, is 0.15 Å from the plane. The atoms of the carboxyl group and C₂ and N₁ are nearly coplanar, the largest displacements from their plane being 0.027 Å (N₁) and -0.033 Å (C₂).

Zinc, and the atoms nearest it (C₂, C₃, C₄, N₁, and N₂) have the smallest and most isotropic vibrations (mean *B* values 2–3 Å²). Towards either extremity of the histidine group—N₃ or O₁ and O₂—the vibrations are larger and more anisotropic; for N₃, the '*B*' value in the *b* axis direction is 2-9 Å² but the values perpendicular to this are in the region of 4 to 6 Å².



Fig. 6. c-axis projection showing the hydrogen bonds around one histidine group and the three water molecules. The hydrogen bonds (dotted lines) are lettered, and their lengths are given in Table 5.

One water molecule oxygen atom (O_5) is on a twofold axis; the others $(O_3 \text{ and } O_4)$ are in general positions. Details of the intricate system of hydrogen bonds are given in Table 5 and Fig. 6. Two hydrogen bonds, *a* and *b*, provide direct links between molecules in the crystal lattice, and there are many other links through water molecules. O₃ and O₅ take part in four

Table 5. Hydrogen bonds

(1)	(2)	(3)	(4)
a	2.762	$N_3 - O_2$ at $\frac{1}{2} - x$, $\frac{1}{2} - y$, $1 - z$	$N_3 - H_7 \dots O_2$
b	2.963	$N_1 - O_1$ at $-x, -y, 1-z$	$N_1 - H_3 \dots \dots N_1$
c	3.008	$N_1 - O_3$ at x, $-y, -\frac{1}{2} + z$	$N_1 - H_2$ O_3
d	2.964	$O_2 - O_3$	O_2 $H_9 - O_3$
e	2.724	$O_2 - O_4$ at $\frac{1}{2} - x$, $\frac{1}{2} - y$, $1 - z$	$O_2 \dots H_{10} - O_4$
f	2.768	$O_3 - O_3$ at $\frac{1}{2} - x$, $\frac{1}{2} - y$, $2 - z$	$O_3 \ldots \frac{1}{2}H_{11} \ldots \frac{1}{2}H_{11} \ldots O_3$
g	2.742	O ₃ O ₅	$O_3 \ldots \frac{1}{2}H_{12} \ldots \frac{1}{2}H_{13} \ldots O_5$
h	2.831	$O_4 - O_4$ at $-x, 1 - y, -z$	$O_4 \ldots \frac{1}{2}H_{14} \ldots \frac{1}{2}H_{14} \ldots O_4$
j	2.771	$O_4 - O_5$ at $x, y, -1 + z$	$O_4 \dots \frac{1}{2}H_{15} \dots \frac{1}{2}H_{16} \dots O_5$

(1) These are the letters used to label the hydrogen bonds in Fig. 6.

(2) Length of the hydrogen bond (Å).

(3) If the hydrogen bond does not join a pair of atoms with the coordinates listed in Table 1 the appropriate equivalent position of the second atom is given.

(4) This allocation of hydrogen atoms and 'half hydrogen atoms' is essential if the space-group is truly centrosymmetric.



Fig. 7. The packing of di(histidino)zinc molecules and water m olecules (open circles) as seen in projection along the c-axis

hydrogen bonds each, while O_4 takes part in only three; O_4 has a significantly larger temperature factor than O_3 and O_5 . Fig. 7 shows the resultant packing of the molecules.

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